

Division - Soil in Space and Time | Commission - Pedometrics

Geostatistical-based index for spatial variability in soil properties

Edemar Appel Neto⁽¹⁾ , Enio Junior Seidel^{(2)*}  and Marcelo Silva de Oliveira⁽¹⁾ 

⁽¹⁾ Universidade Federal de Lavras, Departamento de Estatística, Lavras, Minas Gerais, Brasil.

⁽²⁾ Universidade Federal de Santa Maria, Departamento de Estatística, Santa Maria, Rio Grande do Sul, Brasil.

ABSTRACT: The assessment of spatial variability of environmental variables such as soil properties is important for site-specific management. A geostatistical index that allows quantifying and characterizing the structure of spatial variability is fundamental in this context. Thus, this study aimed to develop a new spatial dependency index, called the Spatial Dependence Measure (SDM) for the spherical, exponential, Gaussian, cubic, pentaspherical, and wave semivariogram models; and comparing it with some of the indexes available in the literature. The SDM is also dimensionless, in the same way as the Spatial Dependence Index (SDI), also considering more parameters of the semivariogram, when compared to the Spatial Dependence Degree (SPD) and Relative Nugget Effect (NE) indexes. In a simulation data study, it is observed that the SDI and SDM indexes showed an advantage over the SPD (or NE). To exemplify the application of the SDM in the proposal for the classification of soil properties, we used estimates of geostatistical parameters presented in the two studies. The results indicate that the SDM can be a measure that, analyzed together with the SDI, can help to improve the description of the spatial variability structure. Thus, this study expands the number of geostatistical-based measures and increases the power of decision on the description of the degree of spatial variability of agricultural and soil attributes.

Keywords: within-field variability, spatial dependence, autocorrelation, semivariogram.

* **Corresponding author:**
E-mail: enioseidel@gmail.com

Received: May 08, 2020

Approved: June 29, 2020

How to cite: Appel Neto E, Seidel EJ, Oliveira MS. Geostatistical-based index for spatial variability in soil properties. Rev Bras Cienc Solo. 2020;44:e0200086.
<https://doi.org/10.36783/18069657rbc20200086>

Copyright: This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided that the original author and source are credited.



INTRODUCTION

Several studies have highlighted the importance of measuring the spatial variability of agricultural and soil properties using geostatistical indexes (Seidel and Oliveira, 2014, 2016; Appel Neto et al., 2018; Santos et al., 2018; Amaral and Della Justina, 2019; Leroux and Tisseyre, 2019). Such indexes are useful to assess the quality of the model fit on the semivariogram (Pazini et al., 2015; Oldoni and Bassoi, 2016; Büttow et al., 2017) and, consequently, to indicate whether kriging interpolation results in good quality maps (Appel Neto et al., 2018). In addition, these indexes allow the comparison of within-field variability in different research situations such as when comparing the variability of different types of soils, chemical or physical properties, different crops, among others.

One of the most common indexes in the Soil Science literature in Brazil to calculate the degree of spatial variability is presented in Cambardella et al. (1994), called the Relative Nugget Effect (NE), relating the nugget effect and the sill parameters. Another existing index is that proposed by Biondi et al. (1994), called the Spatial Dependence Degree (SPD), relating the contribution and the sill parameters.

An alternative for the inclusion of the range parameter into a measure of spatial dependence is the use of integral scales J1 and J2 (Russo and Jury, 1987). Han et al. (1994) presented a closed form for the integral scale J1, called Mean Correlation Distance (MCD), considering the contribution, sill, and range parameters. Despite considering more aspects of the semivariogram, integral scales are given in a unit of distance measurement as meters (m) or kilometers (km), which makes it difficult to propose a categorization to classify spatial dependence.

A Spatial Dependence Index (SDI) was proposed by Seidel and Oliveira (2014, 2016) and Appel Neto et al. (2018), which is a dimensionless index (free of measurement units), inspired by integral scale J1 (Russo and Jury, 1987) and based on spatial correlation area. This SDI index takes a specific form for each semivariogram model considered, being proposed for the spherical, exponential, Gaussian (Seidel and Oliveira, 2014, 2016), cubic, pentaspherical, and wave models (Appel Neto et al., 2018). For its construction, the SDI index considers the following parameters of the semivariogram: contribution, sill, range, and half of the maximum distance between sampled points. The spherical, exponential, Gaussian, cubic, pentaspherical, and wave semivariogram models were studied; according to Olea (2006), they are the most used by researchers.

In the matter of geostatistical indexes for measuring spatial variability, there is still room to expand this knowledge. Thus, following the same idea as Seidel and Oliveira (2014, 2016) and Appel Neto et al. (2018) in the construction of the SDI, the aim of this study was to develop a new spatial variability index, called the Spatial Dependence Measure (SDM), inspired by integral scale J2 (Russo and Jury, 1987), and comparing it with some of the indexes already exist in the literature.

MATERIALS AND METHODS

Equations 1 and 2 show the measurements NE (Cambardella et al., 1994) and SPD (Biondi et al., 1994), respectively.

$$NE = \frac{C_0}{C_0 + C_1} 100 \quad \text{Eq. 1}$$

$$SPD = \frac{C_1}{C_0 + C_1} 100 \quad \text{Eq. 2}$$

in which C_0 is the nugget effect; C_1 is the contribution; $C_0 + C_1$ is the sill; NE and SPD are complementary in the sense that $SPD = 100 - NE$. Thus, it was decided to use only the SPD in the analyses.

Equations 3 to 8 show the expressions of the SDI index for the spherical, exponential, Gaussian (Seidel and Oliveira, 2016), cubic, pentaspherical, and wave models (Appel Neto et al., 2018), respectively.

$$SDI_{spherical} = 0.375 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 3}$$

$$SDI_{exponential} = 0.317 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 4}$$

$$SDI_{gaussian} = 0.504 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 5}$$

$$SDI_{cubic} = 0.365 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 6}$$

$$SDI_{pentaspherical} = 0.312 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 7}$$

$$SDI_{wave} = 0.589 \left(\frac{C_1}{C_0 + C_1} \right) \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 8}$$

in which C_1 is the contribution; $C_0 + C_1$ is the sill; a is the range; MD is the maximum distance. The values 0.375, 0.317, 0.504, 0.365, 0.312, and 0.589 are the respective model factors (MF) of each of the semivariogram models. The $\min \{ \}$ function is used to adjust the fact that the component $\frac{a}{0.5 MD}$ is not necessarily limited in the amplitude from zero to one.

The SDM index was proposed following the same method as Seidel and Oliveira (2014, 2016) and Appel Neto et al. (2018). First, the spatial correlation measure (SCM) is calculated. In this case, what differentiates in the calculation of the SCM in relation to the integral scale J_2 is that in the SCM, the integration limit used is from zero until the value of the range (a). Equation 9 shows the spatial correlation measure obtained in general.

$$SCM = \left\{ 2 \int_0^a \rho(h) h dh \right\}^{\frac{1}{2}} = \left\{ 2 \int_0^a \frac{(C_0 + C_1) - \gamma(h)}{C_0 + C_1} h dh \right\}^{\frac{1}{2}} = MF \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} a \quad \text{Eq. 9}$$

in which $\rho(h)$ is the correlogram function; $\gamma(h)$ is the semivariogram function; h is the distance between sampled points; C_0 is the nugget effect; C_1 is the contribution; $C_0 + C_1$ is the sill; a is the range; MF is the model factor (specific to each semivariogram model).

Then, the SCM is multiplied by the inverse of half of the greatest distance between the georeferenced points in the sampling grid, according to equation 10. Half of the greatest distance between points was used in the same way as in Seidel and Oliveira (2016) and Appel Neto et al. (2018).

$$SCM \left(\frac{1}{0.5 MD} \right) = MF \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} a \left(\frac{1}{0.5 MD} \right) \quad \text{Eq. 10}$$

in which C_1 is the contribution; $C_0 + C_1$ is the sill; a is the range; $0.5 MD$ is half of the maximum distance between sampled points; MF is the model factor (specific to each semivariogram model).

Then, by rearranging the equation 10, the Spatial Dependence Measure (SDM) is obtained. Equations 11 to 16 show the SDM index for the spherical, exponential, Gaussian, cubic, pentaspherical, and wave models, respectively.

$$SDI_{spherical} = 0.447 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 11}$$

$$SDI_{exponential} = 0.422 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 12}$$

$$SDI_{gaussian} = 0.563 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 13}$$

$$SDI_{cubic} = 0.408 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 14}$$

$$SDI_{pentaspherical} = 0.378 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 15}$$

$$SDI_{wave} = 0.637 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 16}$$

in which C_1 is the contribution; $C_0 + C_1$ is the sill; a is the range; MD is the maximum distance. The values 0.447, 0.422, 0.563, 0.408, 0.378, and 0.637 are the respective model factors (MF) of each of the semivariogram models. The $\min \{ \}$ function is used to adjust the fact that the component $\frac{a}{0.5 MD}$ is not necessarily limited in the amplitude from zero to one.

To carry out the classification of the SDM, a methodology adapted from Seidel and Oliveira (2016) and Appel Neto et al. (2018) was used. Values were generated for the components $\left(\frac{C_1}{C_0 + C_1} \right)$ and $\left(\frac{a}{0.5 MD} \right)$, from 0.05 to 1.00, varying by 0.05. Afterward, these values were combined by multiplications $\left[\left(\frac{C_1}{C_0 + C_1} \right) \left(\frac{a}{0.5 MD} \right) \right]$, which generated a vector of 400 values that was increased by a zero value. Thus, the vector of 401 values between 0 and 1 was multiplied by MF100 for each model. Finally, the median and the third quartile of each vector (one for each semivariogram model) were considered as cuts to categorize the SDM and classify the spatial dependence as weak, moderate, and strong, as shown in table 1.

To evaluate the performance of the SDM and compare it with some of the indexes used in the literature, 25 scenarios of spatial variability were simulated in the geoR package

Table 1. Amplitude of values and proposed classification for the Spatial Dependence Measure (SDM)

Model	Amplitude	Classification		
		Weak	Moderate	Strong
Spherical	0 to 44.70	$0 \leq \text{SDM} \leq 14$	$14 < \text{SDM} \leq 24$	$24 < \text{SDM} \leq 44.70$
Exponential	0 to 42.20	$0 \leq \text{SDM} \leq 14$	$14 < \text{SDM} \leq 22$	$22 < \text{SDM} \leq 42.20$
Gaussian	0 to 56.30	$0 \leq \text{SDM} \leq 18$	$18 < \text{SDM} \leq 30$	$30 < \text{SDM} \leq 56.30$
Cubic	0 to 40.80	$0 \leq \text{SDM} \leq 13$	$13 < \text{SDM} \leq 22$	$22 < \text{SDM} \leq 40.80$
Pentaspherical	0 to 37.80	$0 \leq \text{SDM} \leq 12$	$12 < \text{SDM} \leq 20$	$20 < \text{SDM} \leq 37.80$
Wave	0 to 63.70	$0 \leq \text{SDM} \leq 21$	$21 < \text{SDM} \leq 34$	$34 < \text{SDM} \leq 63.70$

(Ribeiro Junior and Diggle, 2001), from R software (R Development Core Team, 2018). The scenarios were composed with the following parameters: contribution values of 10, 25, 50, 75, and 90 % of sill = 50; range values of 10, 25, 50, 75, and 90 % of $0.5MD = 70.71$ m, in at 100×100 m sampling grid. Each scenario was replicated 100 times to mitigate possible variations in the simulation algorithm. With the 100 values generated from each scenario, the SPD, SDI, SDM and, as performance measures, the Mean Squared Error (MSE) and the Kriging Variance (KV) generated by cross-validation were calculated. Finally, Pearson's correlations between the indexes and performance measures were calculated. In the case of a high spatial dependence structure, there are higher values in the SPD, SDI, and SDM indexes and lower values for the MSE and KV, so those negative correlations between the indexes and performance measures are expected. The results of the correlations are shown in table 2.

To exemplify the application of the SDM in the proposal for classification of soil properties, we use estimates of geostatistical parameters presented in the studies by Oldoni and Bassoi (2016) and Guedes et al. (2020). The authors used the SPD (or NE) and SDI indexes. From this, we also calculate the SDM index and apply its proposed classification. These results are shown in table 3.

RESULTS AND DISCUSSION

The SDM differs from the SDI in the values of the model factor (MF) and also by the inclusion of a square root in the component $\frac{C_1}{C_0 + C_1}$ to give more weight to this component in the measurement of spatial variability. In addition, the SDM is also dimensionless (does not depend on units of measurement), in the same way as the SDI, also considering more parameters of the semivariogram, when compared to the NE and SPD indexes. The range parameter allows the evaluation of the spatial variability in the horizontal direction of the semivariogram, and the contribution and the sill parameters allow the evaluation of the spatial variability in the vertical direction of the semivariogram (Santos et al., 2018). The SDI and SDM indexes capture these aspects well in the whole area of the semivariogram graph, in other words, in both directions (horizontal and vertical) within the graph area, that is, in the direction of the horizontal axis of the semivariogram graph, and in the direction of the vertical axis of the semivariogram graph.

In general, in table 2, of the ten possible correlations between each index and performance measures, for the SPD there are six of them as strong, for the SDI there are eight of them as strong, and for the SDM also there are eight of them as strong. Thus, it is observed that the SDI and SDM indexes showed an advantage over the SPD. In addition, SDI was slightly better than SDM. Seidel and Oliveira (2014) found that the SDI had a slight advantage over the SPD, with a higher frequency of good correlations with the mean squared error of cross-validation. However, Amaral and Della Justina (2019) observed that the NE (or SPD) and SDI indexes did not perform as well as cross-validation measures in assessing the quality of kriging maps. In the sense of the relationship between the

Table 2. Correlations between the Spatial Dependence Degree (SPD), Spatial Dependence Index (SDI), and Spatial Dependence Measure (SDM), and between Mean Squared Error (MSE) and Kriging Variance (KV) of the cross-validation, in semivariogram models

Indexes	Spherical		Exponential		Gaussian		Cubic		Wave	
	MSE	KV	MSE	KV	MSE	KV	MSE	KV	MSE	KV
SPD	-0.67	-0.44	-0.92	-0.70	-0.79	-0.77	-0.63	-0.34	-0.77	-0.78
SDI	-0.84	-0.97	-0.91	-0.97	-0.79	-0.83	-0.86	-0.95	-0.51	-0.55
SDM	-0.80	-0.94	-0.90	-0.95	-0.72	-0.77	-0.81	-0.91	-0.45	-0.50

Strong correlations: -1.00 to -0.70; moderate correlations: -0.69 to -0.30. The pentaspherical model is not implemented in the geoR package (Ribeiro Junior and Diggle, 2001) so that the simulation was not performed.

Table 3. Spatial Dependence Degree (SPD), Spatial Dependence Index (SDI), Spatial Dependence Measure (SDM), and classifications generated for some soil properties

Properties ⁽¹⁾	Model ⁽²⁾	Range	SPD	SDI	SDM	SPD classification	SDI classification	SDM classification
		m	%					
Sand ⁽³⁾	Exp	85.5	50.2	13.7	25.7	Moderate	Strong	Strong
Silt ⁽³⁾	Gaus	55.5	35.5	10.0	18.8	Moderate	Moderate	Moderate
Clay ⁽³⁾	Sph	40.6	79.9	12.2	16.3	Strong	Moderate	Moderate
AW ⁽³⁾	Sph	146.2	84.6	31.7	41.1	Strong	Strong	Strong
SD ⁽³⁾	Gaus	60.6	75.9	23.3	29.9	Strong	Strong	Moderate
57 DAP ⁽³⁾	Sph	36.0	46.3	6.0	10.5	Moderate	Weak	Weak
60 DAP ⁽³⁾	Sph	90.3	53.4	17.3	28.2	Moderate	Strong	Strong
100-101 DAP ⁽³⁾	Sph	46.9	47.6	8.0	13.8	Moderate	Moderate	Weak
63 DAP ⁽³⁾	Sph	99.0	62.4	22.1	33.3	Moderate	Strong	Strong
78 DAP ⁽³⁾	Sph	35.8	74.1	9.5	13.2	Moderate	Moderate	Weak
91 DAP ⁽³⁾	Gaus	25.6	99.9	12.3	13.7	Strong	Moderate	Weak
Carbon ⁽⁴⁾	Gaus	254.9	47.5	6.9	11.2	Moderate	Weak	Weak
Calcium ⁽⁴⁾	Gaus	639.9	29.0	10.6	22.0	Moderate	Moderate	Weak
Magnesium ⁽⁴⁾	Gaus	685.5	16.0	6.3	17.5	Weak	Weak	Weak
pH ⁽⁴⁾	Exp	300.0	35.1	8.3	18.6	Moderate	Moderate	Moderate

⁽¹⁾ AW: available water; SD: soil density; DAP: days after pruning. ⁽²⁾ Exp: exponential; Gaus: Gaussian; Sph: spherical. ⁽³⁾ Soil properties presented in Oldoni and Bassoi (2016). ⁽⁴⁾ Soil properties presented in Guedes et al. (2020).

indexes and the range parameter, Santos et al. (2018) found that SDI had a moderate to a strong positive correlation with range parameter; and, the SPD had a weak to moderate negative correlation with range parameter.

Some researchers use metrics together to better assess spatial variability and optimize decision-making: Taylor et al. (2007) using the NE and the MCD; Souza et al. (2008) using the NE and the integral scale J2; Oldoni and Bassoi (2016) using SPD and SDI; Amaral and Della Justina (2019) and Guedes et al. (2020) using the NE and SDI. These findings show the need for further studies to propose and evaluate the performance of the indexes, mainly for the SDM that is being proposed.

From table 3, it can be seen that the SPD index generates four strong classifications, ten moderate classifications and one weak. The SDI generates five strong classifications, seven moderate, and three weak. While the SDM index generates four strong ratings, four moderate, and seven weak. Considering a joint assessment of the three indexes, it is possible to verify that sand, available water, soil density, 60 days after pruning (DAP), and 63 DAP were classified as strong in at least two of the indices. The properties silt, clay, 100-101 DAP, 78 DAP, calcium, and pH were classified as moderate in at least two of the indexes. The properties 57 DAP, carbon, and magnesium were classified as weak by at least two of the indexes. However, the 91 DAP property had the three discordant classifications.



CONCLUSIONS




The Spatial Dependence Measure (SDM) can be a measure that, analyzed together with the Spatial Dependence Index (SDI), can help to improve the description and classification of the spatial variability structure. Thus, this study expands the number of geostatistical-based measures and increases the power of decision on the description of the degree of spatial variability of agricultural and soil properties.




ACKNOWLEDGEMENTS

The authors would like to thank FAPEMIG and CNPq for their support in carrying out this research.




AUTHOR CONTRIBUTIONS



Conceptualization:  Enio Júnior Seidel (equal) and  Marcelo Silva de Oliveira (equal).



Methodology:  Edemar Appel Neto (equal),  Enio Júnior Seidel (equal), and  Marcelo Silva de Oliveira (equal).

Formal analysis:  Edemar Appel Neto (lead),  Enio Júnior Seidel (supporting), and  Marcelo Silva de Oliveira (supporting).

Writing - original draft:  Edemar Appel Neto (equal) and  Enio Júnior Seidel (equal).

Writing - review and editing:  Edemar Appel Neto (equal),  Enio Júnior Seidel (equal), and  Marcelo Silva de Oliveira (equal).

Supervision:  Enio Júnior Seidel (equal) and  Marcelo Silva de Oliveira (equal).

Funding acquisition:  Edemar Appel Neto (equal) and  Marcelo Silva de Oliveira (equal).

REFERENCES

- Amaral LR, Della Justina DD. Spatial dependence degree and sampling neighborhood influence on interpolation process for fertilizer prescription maps. *Eng Agric.* 2019;39:85-95. <https://doi.org/10.1590/1809-4430-eng.agric.v39nep85-95/2019>
- Appel Neto E, Barbosa IC, Seidel EJ, Oliveira MS. Spatial dependence index for cubic, pentaspherical and wave semivariogram models. *Bol Cienc Geod.* 2018;24:142-51. <https://doi.org/10.1590/s1982-21702018000100010>
- Biondi F, Myers DE, Avery CC. Geostatistically modeling stem size and increment in an old-growth forest. *Can J Forest Res.* 1994;24:1354-68. <https://doi.org/10.1139/x94-176>
- Büttow GT, Pazini JB, Seidel EJ, Silva FF, Grutzmacher AD, Martins JFS. Relationship between the occurrence of the rice water weevil and water depth in flooded rice crop. *Pesq Agropec Bras.* 2017;52:557-60. <https://doi.org/10.1590/s0100-204x2017000700010>
- Cambardella CA, Moorman TB, Parkin TB, Karlen DL, Novak JM, Turco RF, Konopka AE. Field-scale variability of soil properties in central Iowa soils. *Soil Sci Soc Am J.* 1994;58:1501-11. <https://doi.org/10.2136/sssaj1994.03615995005800050033x>
- Guedes LPC, Bach RT, Uribe-Opazo MA. Nugget effect influence on spatial variability of agricultural data. *Eng Agric.* 2020;40:96-104. <https://doi.org/10.1590/1809-4430-eng.agric.v40n1p96-104/2020>
- Han S, Hummel JW, Goering CE, Cahn MD. Cell size selection for site-specific crop management. *Trans Amer Soc Agr Eng.* 1994;37:19-26. <https://doi.org/10.13031/2013.28048>
- Leroux C, Tisseyre B. How to measure and report within-field variability: a review of common indicators and their sensitivity. *Precis Agric.* 2019;20:562-90. <https://doi.org/10.1007/s11119-018-9598-x>
- Oldoni H, Bassoi LH. Delineation of irrigation management zones in a Quartzipsamment of the Brazilian semiarid region. *Pesq Agropec Bras.* 2016;51:1283-94. <https://doi.org/10.1590/s0100-204x2016000900028>
- Olea RA. A six-step practical approach to semivariogram modeling. *Stoch Env Res Risk A.* 2006;20:307-18. <https://doi.org/10.1007/s00477-005-0026-1>
- Pazini JB, Botta RA, Seidel EJ, Silva FF, Martins JFS, Barrigossi JAF, Rubenich R. Geostatistics applied to the study of the spatial distribution of *Tibraca limbativentris* in flooded rice fields. *Cienc Rural.* 2015;45:1006-12. <https://doi.org/10.1590/0103-8478cr20140841>

R Development Core Team. R: A language and environment for statistical computing. R Foundation for Statistical Computing. Vienna, Austria; 2018. Available from: <http://www.R-project.org/>.

Ribeiro Junior PJ, Diggle PJ. geoR: a package for geostatistical analysis. *R News*. 2001;1:15-8.

Russo D, Jury W. A theoretical study of the estimation of the correlation scale in spatially variable fields: 1. Stationary fields. *Water Resour Res*. 1987;23:1257-68. <https://doi.org/10.1029/WR023i007p01257>

Santos ELE, Seidel EJ, Pazini JB, Oliveira MS, Appel Neto E, Barbosa IC. Some aspects about the spatial dependence index for variability of soil attributes. *Cienc Rural*. 2018;48:e20170710. <https://doi.org/10.1590/0103-8478cr20170710>

Seidel EJ, Oliveira MS. Novo índice geoestatístico para a mensuração da dependência espacial. *Rev Bras Cienc Solo*. 2014;38:699-705. <https://doi.org/10.1590/S0100-06832014000300002>

Seidel EJ, Oliveira MS. A classification for a geostatistical index of spatial dependence. *Rev Bras Cienc Solo*. 2016;40:e0160007. <https://doi.org/10.1590/18069657rbcs20160007>

Souza ES, Antonio ACD, Jaramillo RA, Netto AM, Montenegro SMGL, Silva EB. Variabilidade espacial dos parâmetros hidrodinâmicos de duas parcelas agrícolas no estado da Paraíba. *Rev Bras Cienc Solo*. 2008;32:1795-804. <https://doi.org/10.1590/S0100-06832008000500001>

Taylor JA, Praat JP, Bollen AF. Spatial variability of kiwifruit quality in orchards and its implications for sampling and mapping. *HortScience*. 2007;42:246-50. <https://doi.org/10.21273/HORTSCI.42.2.246>

Errata RBCS 2020-0086

In the article “Geostatistical-based index for spatial variability in soil properties” [Rev Bras Cienc Solo. 2020;44: e0200086. DOI: 10.36783/18069657rbc20200086], on page 4 (Equations 11 to 16), where it is presented:

$$SDI_{spherical} = 0.447 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 11}$$

$$SDI_{exponential} = 0.422 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 12}$$

$$SDI_{gaussian} = 0.563 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 13}$$

$$SDI_{cubic} = 0.408 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 14}$$

$$SDI_{pentaspherical} = 0.378 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 15}$$

$$SDI_{wave} = 0.637 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 16}$$

It should be presented:

$$SDM_{spherical} = 0.447 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 11}$$

$$SDM_{exponential} = 0.422 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 12}$$

$$SDM_{gaussian} = 0.563 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 13}$$

$$SDM_{cubic} = 0.408 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 14}$$

$$SDM_{pentaspherical} = 0.378 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 15}$$

$$SDM_{wave} = 0.637 \left(\frac{C_1}{C_0 + C_1} \right)^{\frac{1}{2}} \min \left\{ 1; \left(\frac{a}{0.5 MD} \right) \right\} 100 \quad \text{Eq. 16}$$

Copyright: This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided that the original author and source are credited.

